























First, I looked at the first equation to solve this problem. This equation was  $a \times b = a$ . Either  $a$  was 0 or  $b$  was 1. Looking at the third equation, I saw it was  $e + f = e$ , so that meant two things:  $f$  was 0; which meant that that zero was already taken, so  $b$  in the first equation would have to equal 1. On the side I wrote out the integers 0-9 and crossed a number out whenever it was taken, or assigned to a particular symbol. At this point only 0 and 1 were crossed out. Then I looked at the second equation. It was in the format  $c \times c + d = e$ , which, simplified, was  $c^2 + d = e$ . Since the greatest value  $e$  could be was a 9, and they were all whole numbers, and 0 and 1 were already taken,  $c$  could only be 2. That made things easier. The equation was now  $4 + d = e$ .  $d$  could have been 3, 4 or 5, and the  $e$  could have been 7, 8 or 9. Skipping the third equation and fourth equations for now, I started on the fifth equation. It was  $e / i + i = j$ . Since all of the numbers had to be whole numbers and 2 was already taken, then  $e$  must be 9 and  $i$  must be 3. Therefore,  $j$  was 6. With only 4, 5, 7, and 8 left,  $g$  in the fourth equation must be 8 and the  $h$  had to be 4.  $d$  in the second equation therefore had to be 5. The only number left was 7, so the  $a$  in the first equation, which could have been anything, must be 7.

REFLECTION: I looked at this problem for a long time and was thoroughly stumped until my dad showed me the first equation and explained the possibilities. We did them together in exactly the same order as I explained in my long answer. The  $a$  in the first equation confused me a little, but when I got down to just 7 left I saw the logic that  $a$  must be 7. I liked this equation and thought it was pretty fun, and I enjoyed the logic twist that it was given. When I had figured it all out, I saw the common sense in it and I thought it was a pretty clever problem.

## Scoring Rubric

A **problem-specific rubric**, to help in assessing student solutions, is available in the Teacher Support Materials on the Problem page when you are logged in as a teacher. As shown above, we consider each category separately when evaluating the students' work, thereby providing more focused information regarding the strengths and weaknesses in the work.

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